

## Student loans

*The objective of this activity is to explore the costs associated with attending college and taking out student loans.*

Congratulations! You just got accepted into your dream college! However, college can be pretty expensive and the tuition at this school is \$25,000 per year. You decide to do some research and apply to financial aid programs to help with these costs.



### Funding your first year of college

You just received your financial aid package in the mail and discovered that you will not receive any scholarships, bummer.

You decide to fully fund your first year of tuition with a Direct unsubsidized federal loan. For this loan, you are charged a **1.057%** loan fee along with an interest rate of **4.99%** which is compounded monthly.

1. Including the loan fee, what is the principal amount of your loan?

We must first determine the loan fee by multiplying \$25,000 by 1.057%. We then add the fee to the original loan amount to determine the principal.

rad CALCULATION	
$25\,000 \times 1.057\%$	264.25
$264.25 + 25\,000$	25\,264.25

The principal for the loan is \$25,264.25.

2. Direct unsubsidized loans start to accrue interest from the date they're disbursed. How much will you owe on this loan at graduation (after 4 years) if no payments have been made?

To determine the balance of the loan after 4 years, we use the **compound interest** formula:

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

rad CALCULATION	
264.25 + 25 000	
	25 264.25
$25\,264.25 \times \left( 1 + \frac{0.0499}{12} \right)^{12(4)}$	
	30 832.72106

You can also use the **Compound interest** section of the **Finance Solver**.

rad SOLVER		rad SOLVER	
Compound interest		Compound interest	
Solving FV (Future value)		N=48 r%=4.99 PV=2.5264 Pmt=0 P/Y=12 C/Y=12	
Calculated values		FV Future value -30832.72106	
N Number of payments	48		
r% Nominal annual rate of interest	4.99		
PV Present value	25264.25		
Pmt Payment each period	0		

After four years, you will owe \$30,832.72.

3. After graduation, you decide to start paying off your student loan by making a \$300 monthly payment. How long, in years, will it take you to pay off this new balance?

Using the **compound interest** section of the **Finance Solver**, we indicate that we are looking for **N**, the number of payments. We then input our rate (4.99), present value (30,832.72), and payment each period (-300).

rad SOLVER	
Compound interest	
Solving N (Number of payments)	
r% Nominal annual rate of interest	4.99
PV Present value	30832.72
Pmt Payment each period	-300
FV Future value	0

rad SOLVER	
Compound interest	
r%=4.99 PV=3.083e4 Pmt=-300 FV=0 P/Y=12...	
Calculated values	
N Number of payments	134.3528506

It will take about 134.35 months after graduation to pay off the loan for your first year. Dividing by 12, we can convert this to years.

rad CALCULATION	
$25\,264.25 \times \left(1 + \frac{0.0499}{12}\right)^{12(4)}$	
30 832.72106	
$\frac{134.3528506}{12}$	11.19607088

It will take approximately 11.2 years after graduation to pay off this loan.

4. If you started making \$300 monthly payments at the start of college, how long would it take you to pay off your loan?

Using the **compound interest** section of the **Finance Solver**, we indicate that we are looking for **N**, the number of payments. We then input our rate (4.99), present value (25,264.25), and payment each period (-300).

rad SOLVER	
Compound interest	
Solving N (Number of payments)	
r% Nominal annual rate of interest	4.99
PV Present value	25264.25
Pmt Payment each period	-300
FV Future value	0

rad SOLVER	
Compound interest	
r%=4.99 PV=2.526e4 Pmt=-300 FV=0 P/Y=12...	
Calculated values	
N Number of payments	103.8809971

It will take about 103.88 months from the start of college to pay off the loan for your first year. Dividing by 12, we can convert this to years.

rad	CALCULATION	
$\frac{134.3528506}{12}$		11.19607088
$\frac{103.8809971}{12}$		8.656749758

It will take approximately 8.66 years from the start of college to pay off this loan.

5. How much would you actually spend on your first year of college for each of these options?

To determine the actual amount spent on the first year of college, multiply the monthly payment (\$300) by the number of months it takes to pay off the loan.

rad	CALCULATION	
12		8.656749758
$300 \times 134.3528506$		40305.85518
$300 \times 103.8809971$		31164.29913

By starting to make payments at the start of college, the total cost of the first year will be \$31,164.30. If you wait until after graduation to make payments, the first year will cost you \$40,305.86.

## Scholarships

While the numbers above may be intimidating, there are over 1.7 million scholarships awarded annually. The U.S. Department of Education awards an estimated \$46 billion in scholarships annually and private sources award over \$7.4 billion in scholarships annually. On average, first time undergraduates who receive government grants and scholarships at a 4-year college receive about \$13,690 annually.<sup>1</sup>

Knowing this, you spent your junior and senior year of high school applying for every scholarship you felt qualified for. Great news! You have now funded 50% of your first year of college through scholarships!

For the remainder of your tuition, you decide to take out a Direct unsubsidized federal loan which charges a **1.057%** loan fee along with an interest rate of **4.99%** which is compounded monthly.

1. Including the loan fee, what is the principal amount of the loan needed to cover half of the tuition for your first year?

With \$12,500 in scholarships, tuition will be \$12,500. We must first determine the loan fee by multiplying \$12,500 by 1.057%. We then add the fee to the original loan amount to determine the principal.

A digital calculator interface with an orange header bar containing the text 'rad' and 'CALCULATION' and a battery icon. The display shows two lines of calculations. The first line shows '25 000 × 50%' followed by the result '12 500' on the right. The second line shows '12 500 + 12 500 × 1.057%' followed by the result '12 632.125' on the right. Below the display is a white input field with a vertical cursor.

The principal for the loan is \$12,632.13.

2. If you started making \$300 monthly payments at the start of college, how long would it take you to pay off your loan?

Using the **compound interest** section of the **Finance Solver**, we indicate that we are looking for **N**, the number of payments. We then input our rate (4.99), present value (12,632.13), and payment each period (-300).

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<sup>1</sup>Education Data Initiative: Scholarship Statistics

rad	SOLVER	
Compound interest		
Solving N (Number of payments)		
r%	4.99	
Nominal annual rate of interest		
PV Present value	12632.13	
Pmt	-300	
Payment each period		
FV Future value	0	

rad	SOLVER	
Compound interest		
r%=4.99 PV=1.263e4 Pmt=-300 FV=0 P/Y=12...		
Calculated values		
N Number of payments	46.38573228	

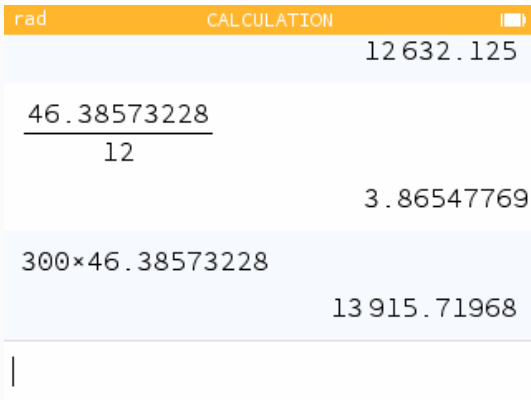
It will take about 46.39 months from the start of college to pay off the loan for the first year. Dividing by 12, we can convert this to years.

rad	CALCULATION	
		12 500
	$12\,500 + 12\,500 \times 1.057\%$	
		12 632.125
	$\frac{46.38573228}{12}$	
		3.86547769

It will take approximately 3.87 years from the start of college to pay off this loan. That means the first year will be paid off before you graduate!

3. How does the actual total cost of the first year of college with a scholarship compare to the cost without a scholarship?

To determine the actual amount spent on the first year of college, multiply the monthly payment (\$300) by the number of months it takes to pay off the loan.



The calculator interface shows the following sequence of operations:

- Initial value: 12 632 . 125
- Operation:  $\frac{46.38573228}{12}$
- Result: 3 . 86547769
- Operation:  $300 \times 46.38573228$
- Result: 13 915 . 71968

With the scholarship and by starting to make payments at the start of college, the total cost of the first year will be \$13,915.72. This is \$17,248.58 less than without a scholarship! And \$26,390.14 less than if you didn't have a scholarship and waited until after college to make payments!

For more information on scholarships and student loans:

- *Fastweb, free scholarship search platform that connects students to scholarships and financial aid tools*
- *US Department of Education: Interest Rates and Fees for Federal Student Loans*